Geometry CC – Mr. Valentino

Unit 11 Lesson 9: Cavalieri's Principle and the Generatrix

Name: ______ Date: ______ Per: _____

Aim: How can we relate 2D to 3D images?

Do Now: Which figure has a larger volume? Why?





1. Which figure has a greater volume? Why?



2. Two stacks of 23 quarters each are shown below. One stack forms a cylinder but the other stack does not form a cylinder. How do their volumes compare?



3. A triangular prism has an isosceles right triangular base with a hypotenuse of $\sqrt{32}$ and a prism height of 15. A square prism has a height of 15 and its volume is equal to that of the triangular prism. What are the dimensions of the square base, in simplest radical form?



Practice Problems



1. If the cylinder is sliced **horizontally**, what are the dimensions of the cross section? Draw a picture of the cross section and label its dimensions.

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What is the area of the cross section in terms of pi?

2. If the cylinder is sliced **vertically** through the middle, what are the dimensions of the cross section? Draw a picture of the cross section and label its dimensions.

What is the area of the cross section?

3. What generatrix could be used to generate the cylinder above? Draw and label the dimensions of ALL the possibilities (make sure to include the axis of rotation)

4. Jenny says that the two prisms DO NOT have the same volume because the cross sections are not the same shape. Renee disagrees; she says that it isn't the shape that has to be the same, it is the area that must be equal. Renee thinks they have the same volume. Who is right and why?



5. If the volume of the cube is 64 cm³, what is the volume of the oblique prism if it has been tilted at 60°?

4 cm	
4 cm 4 cm 4 cm	Volume:
planation:	

6. Find the volume of the cone, to the nearest tenth.



7. You are given the generatrix below. Draw the 3D shape created when rotating it about the axis. Label the dimensions.



8. If the base is doubled and the height halved, what are the dimensions of the new solid? Draw and label its dimensions:

9. What would the vertical cross section look like? Draw and label its dimensions. What's its area?

10. What could be the length of the slant height of the new generatrix?

11. If the following generatrix was dilated by a scale factor of 3, what would be the result of rotating it around the given axis? Draw and label its new dimensions.



12. What would be the dimensions of the vertical and horizontal cross sections? Draw and label them below.

13. Find the areas of each of the cross sections.