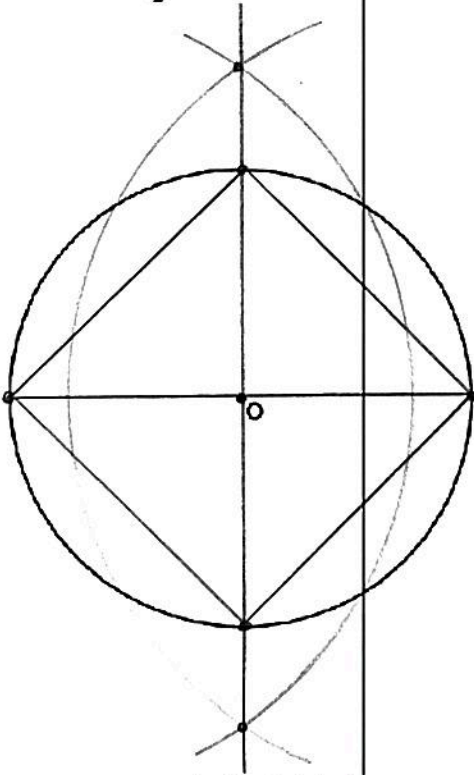
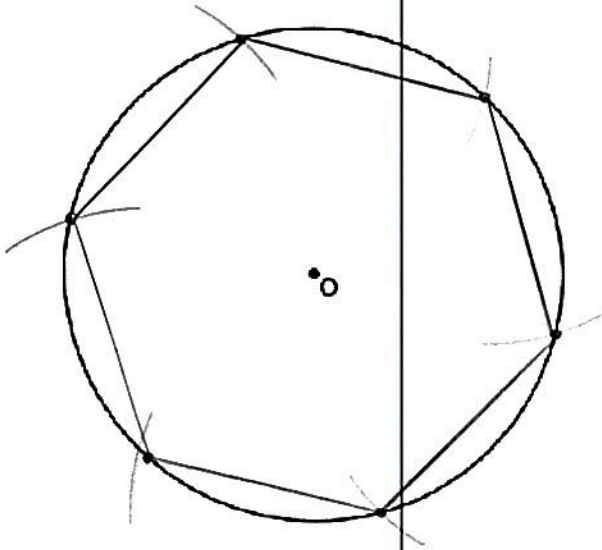


Topic 1: Constructions

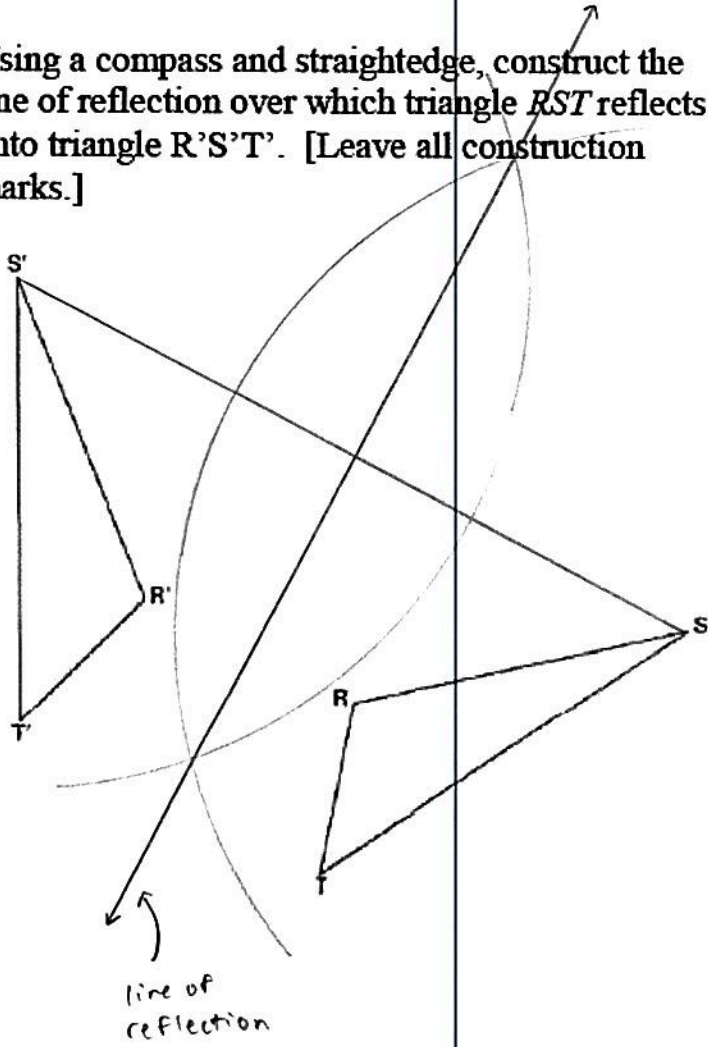
1. Using a straightedge and compass, construct a square inscribed in circle O below. [Leave all construction marks.]



2. Using a compass and straightedge, construct a regular hexagon inscribed in circle O below. Label it $ABCDEF$. [Leave all construction marks.]



3. Using a compass and straightedge, construct the line of reflection over which triangle RST reflects onto triangle $R'S'T'$. [Leave all construction marks.]

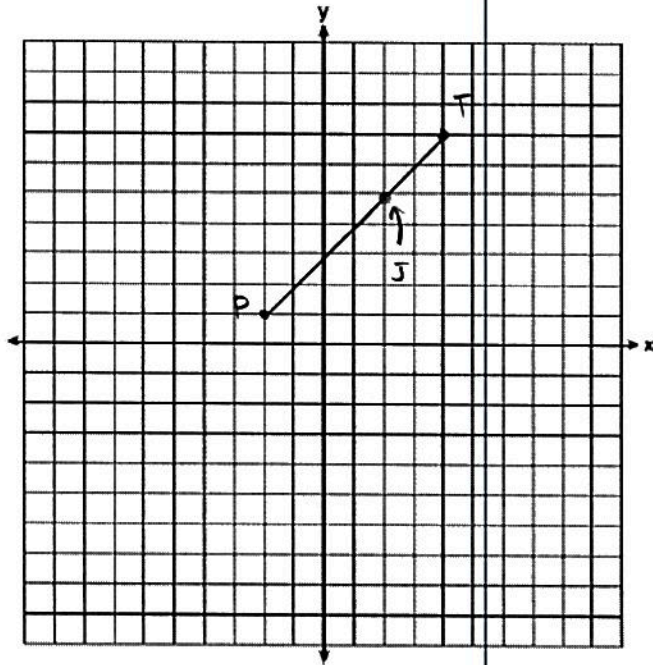


Topic 2: Lines & Angles

1. The endpoints of \overline{DEF} are $D(1,4)$ and $F(16,14)$.
Determine and state the coordinates of point E , if
 $DE:EF = 2:3$.

$$\begin{aligned} & (x_1 + k(x_2 - x_1), y_1 + k(y_2 - y_1)) \\ & (1 + \frac{2}{5}(16 - 1), 4 + \frac{2}{5}(14 - 4)) \\ & (1 + \frac{2}{5}(15), 4 + \frac{2}{5}(10)) \\ & (1 + 6, 4 + 4) \\ & (7, 8) \end{aligned}$$

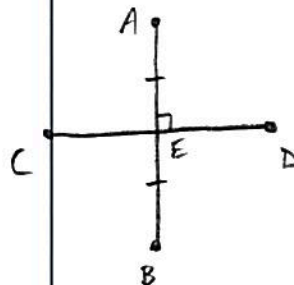
2. Directed line segment PT has endpoints whose coordinates are $P(-2,1)$ and $T(4,7)$. Determine the coordinates of point J that divides the segment in the ratio 2 to 1. [The use of the set of axes below is optional.]



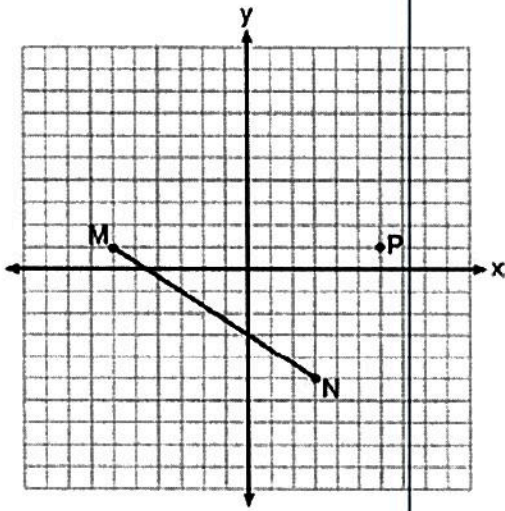
$$\begin{aligned} & (-2 + \frac{2}{3}(4 - (-2)), 1 + \frac{2}{3}(7 - 1)) \\ & (-2 + \frac{2}{3}(6), 1 + \frac{2}{3}(6)) \\ & (-2 + 4, 1 + 4) \\ & (2, 5) \end{aligned}$$

3. Segment CD is the perpendicular bisector of \overline{AB} at E . Which pair of segments does *not* have to be congruent?

- 1 $\overline{AD}, \overline{BD}$
- 2 $\overline{AC}, \overline{BC}$
- 3 $\overline{AE}, \overline{BE}$
- ④ $\overline{DE}, \overline{CE}$



4. Given \overline{MN} shown below, with $M(-6, 1)$ and $N(3, -5)$, what is an equation of the line that passes through point $P(6, 1)$ and is parallel to \overline{MN} ?



$$\begin{aligned} \text{slope}_{MN} &= \frac{\Delta y}{\Delta x} \\ &= \frac{-5-1}{3-(-6)} = \frac{-6}{9} = -\frac{2}{3} \end{aligned}$$

$$y = mx + b$$

$$y = -\frac{2}{3}x + b$$

$$1 = -\frac{2}{3}(6) + b$$

$$1 = -\frac{12}{3} + b$$

$$1 = -4 + b$$

$$5 = b$$

$$y = -\frac{2}{3}x + 5$$

- ① $y = -\frac{2}{3}x + 5$
 2 $y = -\frac{2}{3}x - 3$
 3 $y = \frac{3}{2}x + 7$
 4 $y = \frac{3}{2}x - 8$

5. Line segment \overline{NY} has endpoints $N(-11, 5)$ and $Y(5, -7)$. What is the equation of the perpendicular bisector of \overline{NY} ?

① $y + 1 = \frac{4}{3}(x + 3)$ $y + 1 = \frac{4}{3}x + 4$
 $y = \frac{4}{3}x + 3$

~~2~~ $y + 1 = -\frac{3}{4}(x + 3)$

3 $y - 6 = \frac{4}{3}(x - 8)$ $y - 6 = \frac{4}{3}x + \frac{32}{3}$

~~4~~ $y - 6 = -\frac{3}{4}(x - 8)$

$$\text{slope}_{NY} = \frac{\Delta y}{\Delta x}$$

$$= \frac{-7-5}{5-(-11)} = \frac{-12}{16} = -\frac{3}{4} \rightarrow \text{negative reciprocal}$$

$$\left(\frac{4}{3}\right)$$

$$y = \frac{4}{3}x + b$$

$$-1 = \frac{4}{3}(-3) + b$$

$$-1 = \frac{-12}{3} + b$$

$$-1 = -4 + b$$

$$3 = b$$

$$y = \frac{4}{3}x + 3$$

Midpoint Formula

$$\left(\frac{x_1 + x_2}{2}, \frac{y_1 + y_2}{2}\right)$$

$$\left(\frac{5 + (-11)}{2}, \frac{-7 + 5}{2}\right)$$

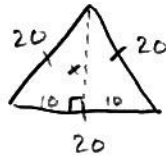
$$\left(\frac{-6}{2}, \frac{-2}{2}\right)$$

must go through this point $\rightarrow (-3, -1)$

Topic 3: Triangles

1. An equilateral triangle has sides of length 20. To the nearest tenth, what is the height of the equilateral triangle?

- 1 10.0
 2 11.5
 ③ 17.3
 4 23.1



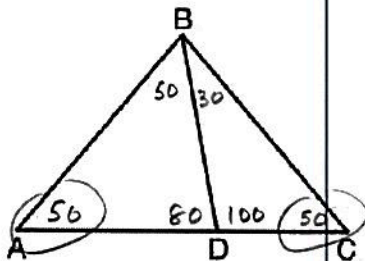
$$10^2 + x^2 = 20^2$$

$$100 + x^2 = 400$$

$$\sqrt{x^2} = \sqrt{300}$$

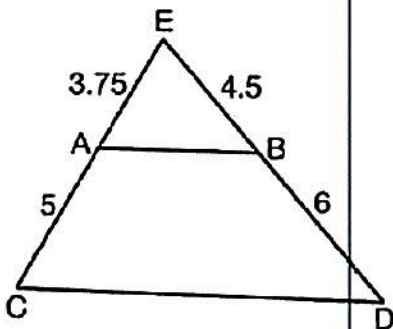
$$x = 17.3$$

2. In the diagram below, $m\angle BDC = 100^\circ$, $m\angle A = 50^\circ$, and $m\angle DBC = 30^\circ$.



Which statement is true?

- $\triangle ABD$ is obtuse.
 $\triangle ABC$ is isosceles. ✓
 $m\angle ABD = 80^\circ$
 $\triangle ABD$ is scalene.
3. In $\triangle CED$ as shown below, points A and B are located on sides CE and ED , respectively. Line segment AB is drawn such that $AE = 3.75$, $AC = 5$, $EB = 4.5$, and $BD = 6$.



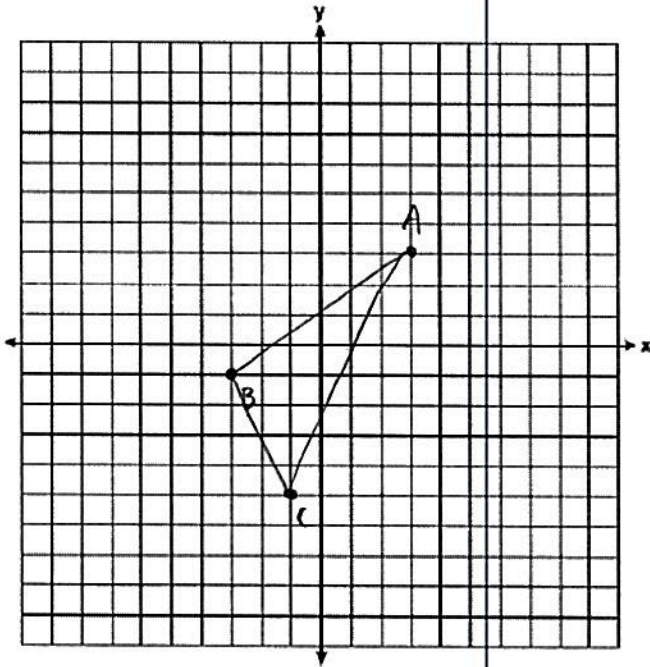
$$\frac{3.75}{5} = \frac{4.5}{6} \quad (\text{Side Splitter})$$

$$.75 = .75$$

Explain why \overline{AB} is parallel to \overline{CD} .

\overline{AB} is parallel to \overline{CD} because it divides the sides (\overline{EC} and \overline{ED}) proportionally.

4. Triangle ABC has vertices with $A(x, 3)$, $B(-3, -1)$, and $C(-1, -4)$. Determine and state a value of x that would make triangle ABC a right triangle. Justify why $\triangle ABC$ is a right triangle. [The use of the set of axes below is optional.]



$$\begin{aligned} \text{slope}_{BC} &= \frac{\Delta y}{\Delta x} \\ &= \frac{-4 - (-1)}{-1 - (-3)} \\ &= \frac{-3}{2} \end{aligned}$$

slope of AB must be neg. reciprocal $(\frac{2}{3})$

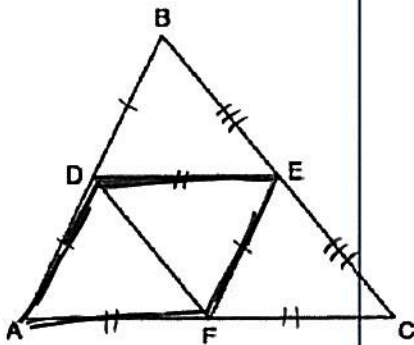
$$\frac{2}{3} = \frac{\Delta y}{\Delta x}$$

$$\frac{2}{3} = \frac{-1 - 3}{-3 - x}$$

$$\frac{2}{3} = \frac{-4}{-3 - x}$$

$(3, 3)$

5. In the diagram below, \overline{DE} , \overline{DF} , and \overline{EF} are midsegments of $\triangle ABC$.



$\triangle ABC$ is a right \triangle because two of its sides have neg. reciprocal slopes which means it has a right \angle .

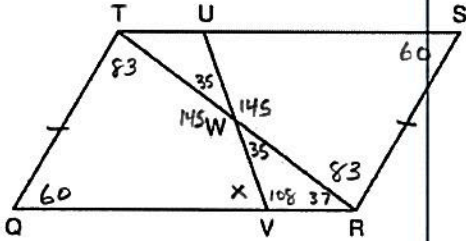
$$\begin{aligned} 2(-3-x) &= -12 \\ -6 - 2x &= -12 \\ -2x &= -6 \\ x &= 3 \end{aligned}$$

The perimeter of quadrilateral $ADEF$ is equivalent to

- 1 $AB + BC + AC$
- 2 $\frac{1}{2}AB + \frac{1}{2}AC$
- 3 $2AB + 2AC$
- ④ $AB + AC$

Topic 4: Quadrilaterals

1. In parallelogram $QRST$ shown below, diagonal \overline{TR} is drawn, U and V are points on \overline{TS} and \overline{QR} , respectively, and \overline{UV} intersects \overline{TR} at W .

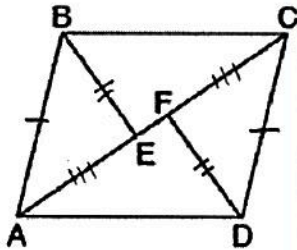


$$60 + 83 + 145 + x = 360$$

$$x = 72$$

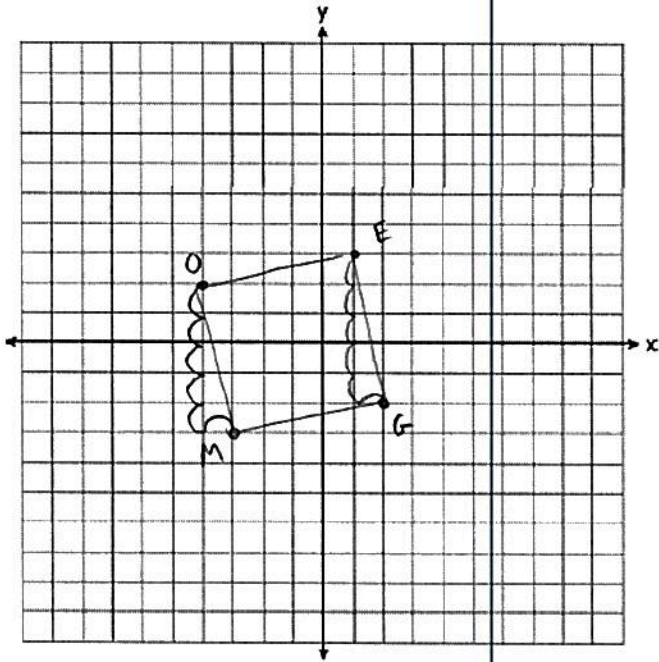
If $m\angle S = 60^\circ$, $m\angle SRT = 83^\circ$, and $m\angle TWU = 35^\circ$, what is $m\angle WVQ$?

- 1 37°
 - 2 60°
 - ③ 72°
 - 4 83°
2. In the diagram below, if $\triangle ABE \cong \triangle CDF$ and \overline{AEFC} is drawn, then it could be proven that quadrilateral $ABCD$ is a



- 1 square
 - 2 rhombus
 - 3 rectangle
 - ④ parallelogram
3. A parallelogram must be a rectangle when its
- 1 diagonals are perpendicular
 - ② diagonals are congruent
 - 3 opposite sides are parallel
 - 4 opposite sides are congruent

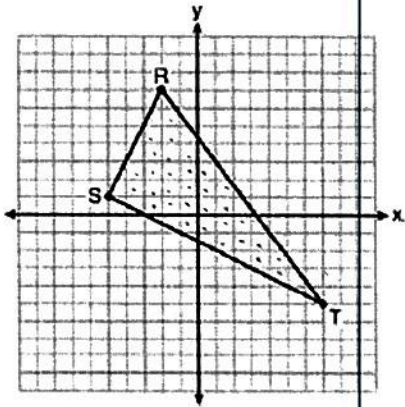
4. In square $GEOM$, the coordinates of G are $(2, -2)$ and the coordinates of O are $(-4, 2)$. Determine and state the coordinates of vertices E and M . [The use of the set of axes below is optional.]



$$M(-3, -3)$$

$$E(1, 3)$$

5. Triangle RST is graphed on the set of axes below.



SHOELACE

$$S(-5, 1)$$

$$R(-2, 7)$$

$$T(7, -5)$$

$$(-5, 1)$$

$$(-5 \cdot 7) + (-2 \cdot -5)$$

$$+ (7 \cdot 1) = |-18| \rightarrow 18$$

$$(1 \cdot -2) + (7 \cdot 7) +$$

$$(-5 \cdot -5) = 72$$

$$\frac{18 + 72}{2} = 45$$

How many square units are in the area of $\triangle RST$?

1 $9\sqrt{3} + 15$

2 $9\sqrt{5} + 15$

3 45

4 90

Even if you count boxes you can rule out 90