

Topic 7: Transformations

1. Line  $l$  is mapped onto line  $m$  by a dilation centered at the origin with a scale factor of 2. The equation of line  $l$  is  $3x - y = 4$ . Determine and state an equation for line  $m$ .

$$3x - y = 4$$

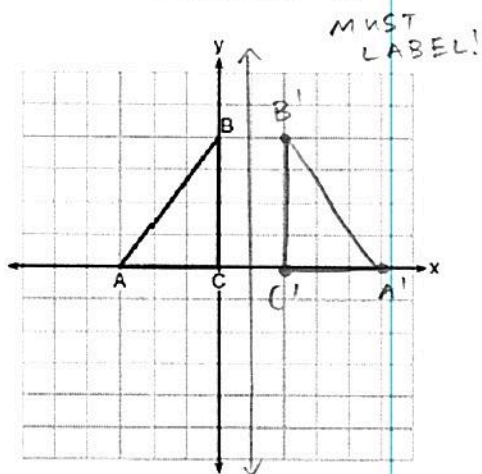
$$3x = y + 4$$

$$-4 \quad -4$$

$$3x - 4 = y$$

line  $m \rightarrow y = 3x - 8$

2. Triangle  $ABC$  is graphed on the set of axes below. Graph and label  $\triangle A'B'C'$ , the image of  $\triangle ABC$  after a reflection over the line  $x = 1$ .

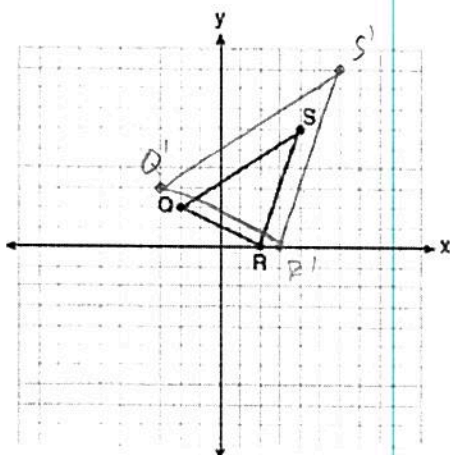


3. A regular hexagon is rotated in a counterclockwise direction about its center. Determine and state the minimum number of degrees in the rotation such that the hexagon will coincide with itself.

Hexagon - 6 sides

$$\frac{360}{6} = 60^\circ$$

4. Triangle  $QRS$  is graphed on the set of axes below.

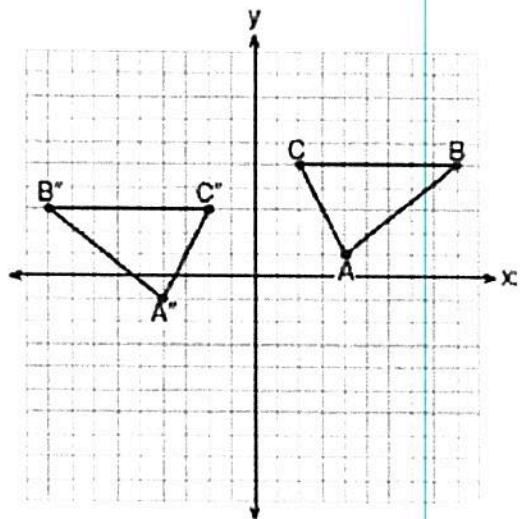


$$\begin{aligned} Q(-2, 2) \cdot \frac{3}{2} &\rightarrow Q'(-3, 3) \\ R(2, 0) \cdot \frac{3}{2} &\rightarrow R'(3, 0) \\ S(4, 6) \cdot \frac{3}{2} &\rightarrow S'(6, 9) \end{aligned}$$

On the same set of axes, graph and label  $\triangle Q'R'S'$ , the image of  $\triangle QRS$  after a dilation with a scale factor of  $\frac{3}{2}$  centered at the origin. Use slopes to explain why  $Q'R' \parallel QR$ .

A dilation preserves slope, so the slopes of  $QR$  and  $Q'R'$  are the same. Since the slopes are equal,  $QR \parallel Q'R'$ .

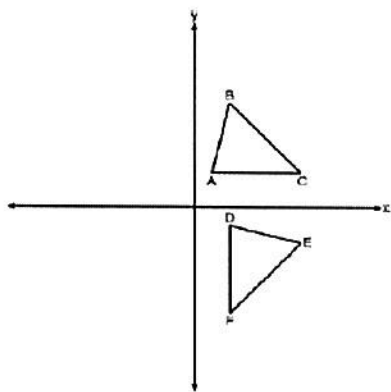
5. The graph below shows  $\triangle ABC$  and its image,  $\triangle A''B''C''$ .



Describe a sequence of rigid motions which would map  $\triangle ABC$  onto  $\triangle A''B''C''$ .

reflection over y-axis followed by Translation down 2 units

6. The image of  $\triangle ABC$  after a rotation of  $90^\circ$  clockwise about the origin is  $\triangle DEF$ , as shown below.

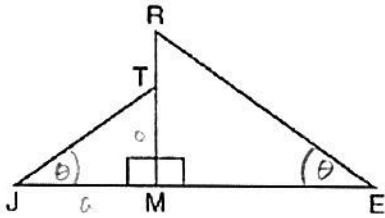


Which statement is true?

- $\overline{BC} \cong \overline{DE}$
- $\overline{AB} \cong \overline{DF}$
- $\angle C \cong \angle E$
- $\angle A \cong \angle D$

Topic 8: Trigonometry

1. In the diagram below,  $\triangle ERM \sim \triangle JTM$ .



Which statement is always true?

- 1  $\cos J = \frac{RM}{RE}$
  - 2  $\cos R = \frac{JM}{JT}$
  - 3  $\tan T = \frac{RM}{EM}$
  - ④  $\tan E = \frac{TM}{JM}$
2. In  $\triangle ABC$ , where  $\angle C$  is a right angle,

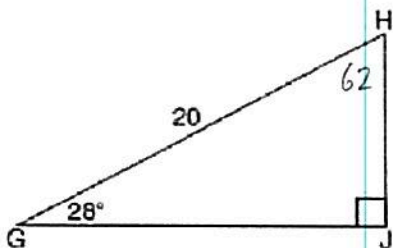
$\cos A = \frac{\sqrt{21}}{5}$ . What is  $\sin B$ ?

- ①  $\frac{\sqrt{21}}{5}$  COFUNCTIONS
- 2  $\frac{\sqrt{21}}{2}$
- 3  $\frac{2}{5}$
- 4  $\frac{5}{\sqrt{21}}$

3. When instructed to find the length of  $HJ$  in right triangle  $HJG$ , Alex wrote the equation

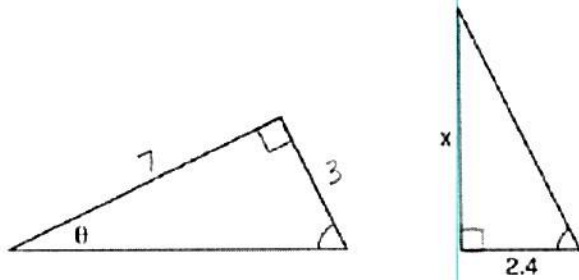
$\sin 28^\circ = \frac{HJ}{20}$  while Marlene wrote  $\cos 62^\circ = \frac{HJ}{20}$ .

Are both students' equations correct? Explain why.



Yes, both students are correct. The two non-right angles in a right  $\triangle$  are complementary and the sine of one of these  $\angle$ 's is equal to the cosine of the other.

4. The diagram below shows two similar triangles.



$$\frac{x}{7} = \frac{2.4}{3}$$

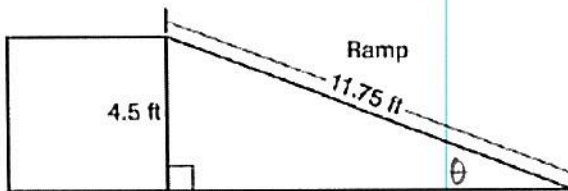
$$3x = 16.8$$

$$x = 5.6$$

If  $\tan \theta = \frac{3}{7}$ , what is the value of  $x$ , to the nearest tenth?

- 1 1.2
- ② 5.6
- 3 7.6
- 4 8.8

5. The diagram below shows a ramp connecting the ground to a loading platform 4.5 feet above the ground. The ramp measures 11.75 feet from the ground to the top of the loading platform.



$$\tan \theta = \frac{4.5}{11.75}$$

$$\theta = 20.95577673$$

$$\theta = 21^\circ$$

Determine and state, to the nearest degree, the angle of elevation formed by the ramp and the ground.