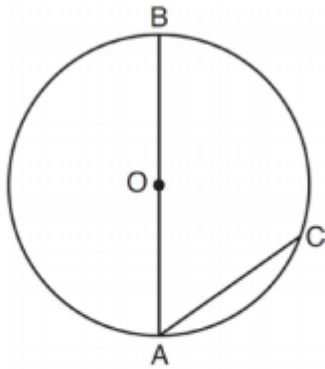




### Angles and Arcs of a Circle

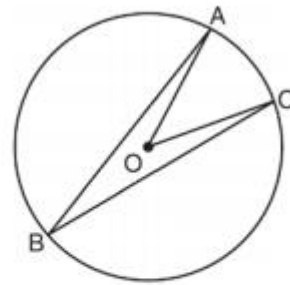
1. As shown in the diagram below,  $\overline{AB}$  is a diameter of circle  $O$ , and chord  $\overline{AC}$  is drawn.



If  $m\angle BAC = 70$ , then  $m\widehat{AC}$  is

- 1) 40
- 2) 70
- 3) 110
- 4) 180

2. In the diagram below of circle  $O$ ,  $m\angle ABC = 24$ .

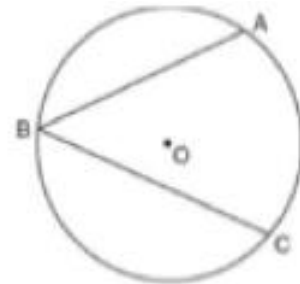


What is the  $m\angle AOC$ ?

- 1) 12
- 2) 24
- 3) 48
- 4) 60

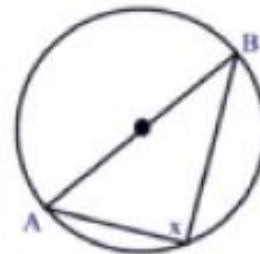
3. In the accompanying diagram of circle  $O$ ,  $m\angle ABC = 2x$  and  $m\widehat{AC} = x + 60$ . Find the value of  $x$ .

- [1] 20      [2] 40      [3] 60      [4] 80



4. Given the circle at the right with diameter  $\overline{AB}$ , find  $x$ .

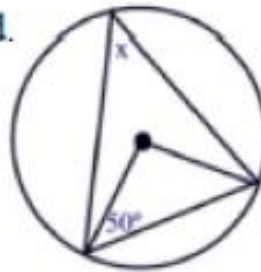
- [1]  $30^\circ$       [2]  $45^\circ$       [3]  $60^\circ$       [4]  $90^\circ$



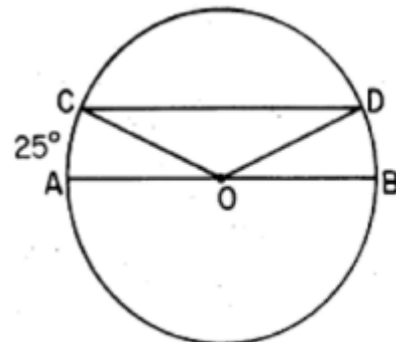
5. Given a circle with the center indicated.

Find  $x$ .

- [1] 100      [3] 50  
[2] 80      [4] 40

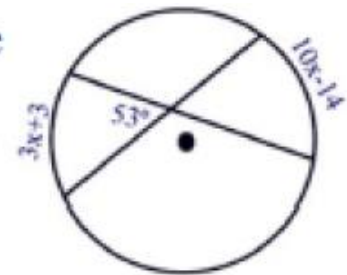


6. In the accompanying diagram, chord  $\overline{CD}$  is parallel to diameter  $\overline{AB}$ . If  $m\widehat{AC} = 25$ , what is  $m\angle COD$ ?



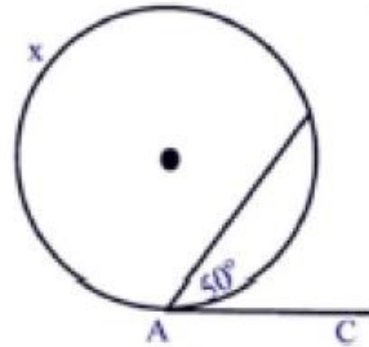
7. Two chords intersect within a circle to form an angle whose measure is  $53^\circ$ . If the intercepted arcs are represented by  $3x + 3$  and  $10x - 14$ , find the measure of larger of these two arcs.

[1] 9                      [2] 13                      [3] 30                      [4] 76



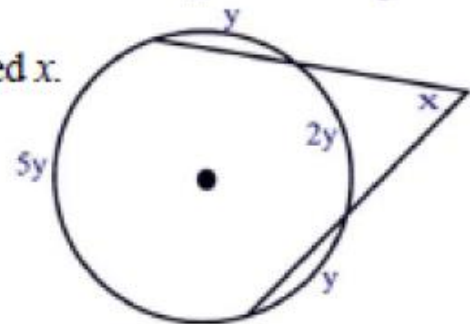
8. Given tangent  $\overline{AC}$  to the circle shown at the right. Find the size of the arc designated by  $x$ .

[1] 25  
[2] 50  
[3] 100  
[4] 260

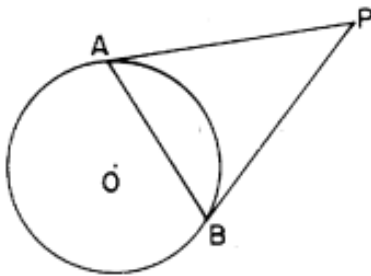


9. Given the two secants shown in the diagram at the right, find the number of degrees in the angle labeled  $x$ .

[1]  $40^\circ$   
[2]  $60^\circ$   
[3]  $80^\circ$   
[4]  $140^\circ$

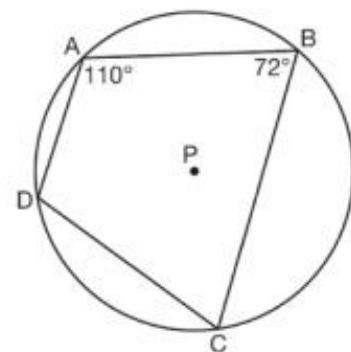
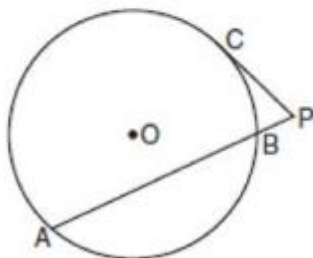


10. In the accompanying diagram,  $\overline{PA}$  and  $\overline{PB}$  are tangents drawn to circle  $O$ . If  $m\angle PBA = 70$ , find  $m\angle P$ .



12. In the diagram below, quadrilateral  $ABCD$  is inscribed in circle  $P$ .

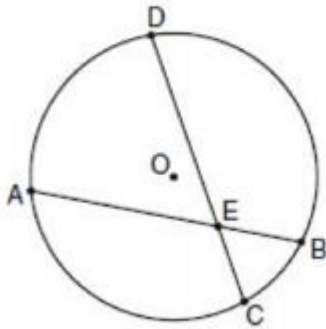
11. In the accompanying diagram of circle  $O$ ,  $\overline{PC}$  is a tangent,  $\overline{PBA}$  is a secant,  $m\widehat{AB} = 132$ , and  $m\widehat{CB} = 46$ . Find  $m\angle P$ .



What is  $m\angle ADC$ ?

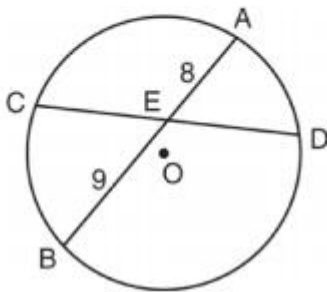
### Chord Length

1. In the diagram of circle  $O$  below, chord  $\overline{AB}$  intersects chord  $\overline{CD}$  at  $E$ ,  $DE = 2x + 8$ ,  $EC = 3$ ,  $AE = 4x - 3$ , and  $EB = 4$ .

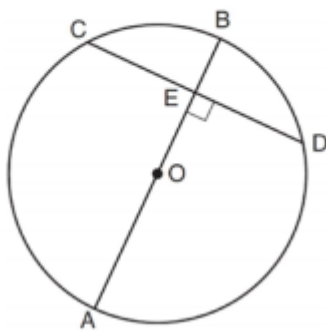


What is the value of  $x$ ?

3. In the diagram below of circle  $O$ , chord  $\overline{AB}$  bisects chord  $\overline{CD}$  at  $E$ . If  $AE = 8$  and  $BE = 9$ , find the length of  $\overline{CE}$  in simplest radical form.

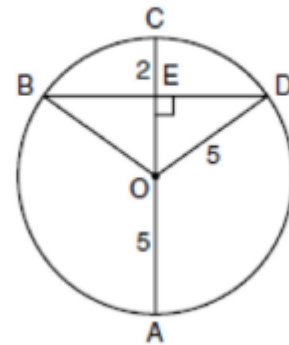


5. In the diagram below of circle  $O$ , diameter  $\overline{AB}$  is perpendicular to chord  $\overline{CD}$  at  $E$ . If  $AO = 10$  and  $BE = 4$ , find the length of  $\overline{CE}$ .



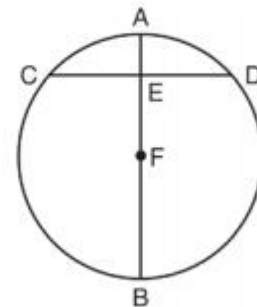
2. Chords  $\overline{AB}$  and  $\overline{CD}$  intersect at point  $E$  in a circle with center at  $O$ . If  $AE = 8$ ,  $AB = 20$ , and  $DE = 16$ , what is the length of  $\overline{CE}$ ?

4. In the diagram below, circle  $O$  has a radius of 5, and  $CE = 2$ . Diameter  $\overline{AC}$  is perpendicular to chord  $\overline{BD}$  at  $E$ .



What is the length of  $\overline{BD}$ ?

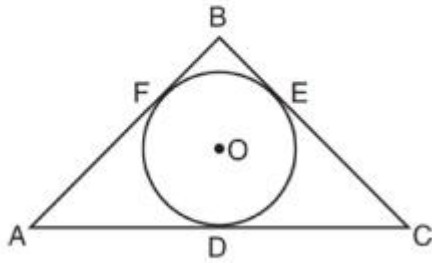
6. In the diagram below, diameter  $\overline{AB}$  bisects chord  $\overline{CD}$  at point  $E$  in circle  $F$ .



If  $AE = 2$  and  $FB = 17$ , then the length of  $\overline{CE}$  is

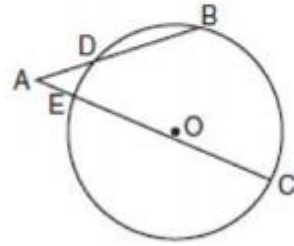
### Tangent-Secant Length

1. In the diagram below,  $\overline{AB}$ ,  $\overline{BC}$ , and  $\overline{AC}$  are tangents to circle  $O$  at points  $F$ ,  $E$ , and  $D$ , respectively,  $AF = 6$ ,  $CD = 5$ , and  $BE = 4$ .

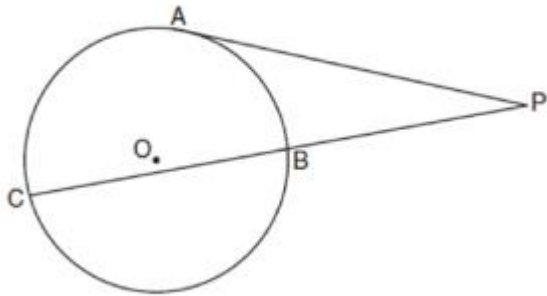


What is the perimeter of  $\triangle ABC$ ?

2. In the accompanying diagram, secant  $\overline{AB}$  intersects circle  $O$  at  $D$ , secant  $\overline{AC}$  intersects circle  $O$  at  $E$ ,  $AE = 4$ ,  $AC = 24$ , and  $AB = 16$ . Find  $AD$ .

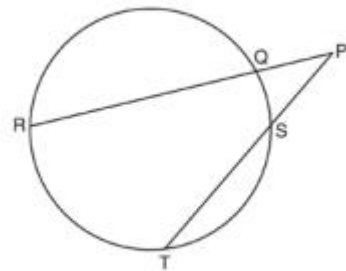


3. In the diagram below, tangent  $\overline{PA}$  and secant  $\overline{PBC}$  are drawn to circle  $O$  from external point  $P$ .



If  $PB = 4$  and  $BC = 5$ , what is the length of  $\overline{PA}$ ?

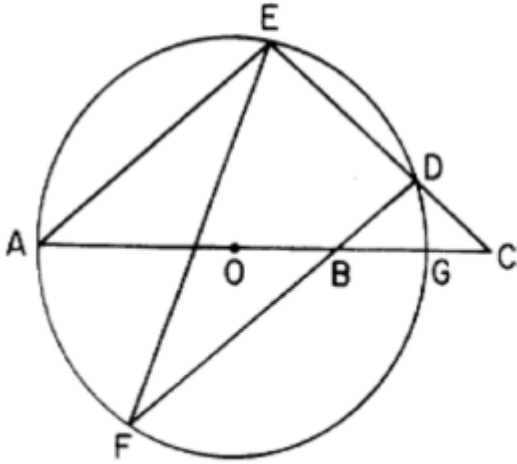
4. In the diagram below, secants  $\overline{PQR}$  and  $\overline{PST}$  are drawn to a circle from point  $P$ .



If  $PR = 24$ ,  $PQ = 6$ , and  $PS = 8$ , determine and state the length of  $\overline{PT}$ .

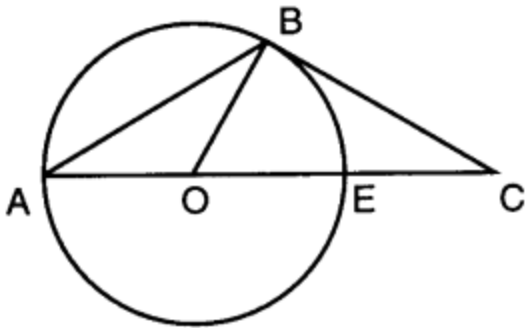
## Super Circles

1. In the accompanying diagram of circle  $O$ ,  $\overline{AE}$  and  $\overline{FD}$  are chords,  $\overline{AOBG}$  is a diameter and is extended to  $C$ ,  $\overline{CDE}$  is a secant,  $\overline{AE} \parallel \overline{FD}$ , and  $m\widehat{AE} : m\widehat{ED} : m\widehat{DG} = 5 : 3 : 1$ .



- $m\widehat{DG} =$   
 $m\angle AEF =$   
 $m\angle DBG =$   
 $m\angle DCA =$   
 $m\angle CDF =$

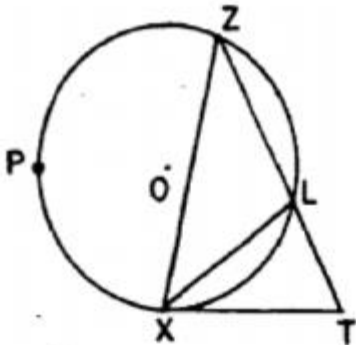
2. In the accompanying diagram of circle  $O$ , diameter  $\overline{AE}$  is extended through  $E$  to  $C$ ; tangent  $\overline{CB}$ , chord  $\overline{AB}$ , and radius  $\overline{OB}$  are drawn; and  $m\widehat{AB} : m\widehat{BE} = 2 : 1$ .



- $m\widehat{AB} =$   
 $m\angle BAC =$   
 $m\angle C =$   
 $m\angle ABC =$

Is  $\triangle OBC$  acute, right, obtuse, or equiangular? Why?

3. Given: circle  $O$ , tangent  $\overline{TX}$ , secant  $\overline{TLZ}$ , chords  $\overline{ZX}$  and  $\overline{XL}$ ,  $m\widehat{XL} : m\widehat{LZ} : m\widehat{XPZ} = 2 : 2 : 5$ .



- $m\widehat{XL} =$   
 $m\angle Z =$   
 $m\angle T =$   
 $m\angle ZXT =$   
 $m\angle XLT =$