

More Recursive Rules

4) If a sequence is defined recursively by $f(1) = 10$ and $f(n) = -f(n-1) + 3$ then find $f(5)$.

5th term
find f(5)

$$\begin{aligned}
 f(1) &= 10 \\
 f(2) &= -f(1) + 3 \\
 f(2) &= -10 + 3 = -7 \\
 f(2) &= -7 \\
 f(3) &= -f(2) + 3 \\
 &= -(-7) + 3 = 7 + 3 = 10 \\
 f(4) &= -f(3) + 3 \\
 &= -(10) + 3 = -7 \\
 f(5) &= -f(4) + 3 \\
 &= -(-7) + 3 = 7 + 3 = 10
 \end{aligned}$$

10, -7, 10, -7, 10

5) A sequence is defined recursively by adding 4 to twice the value of the previous term. Write a recursive rule for this sequence if the first term is 15.

$$\begin{aligned}
 \textcircled{1} \quad a_1 &= 15 \\
 \textcircled{2} \quad a_n &= 2a_{n-1} + 4
 \end{aligned}$$

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 \textcircled{1} \quad f(1) &= 15 \\
 \textcircled{2} \quad f(n) &= 2f(n-1) + 4
 \end{aligned}$$

CONCLUSION!

When creating a sequence using a recursive rule, it is important to understand that each term of the sequence is found using the PREVIOUS term. If the n th term of the sequence is denoted by a_n then the previous term is a_{n-1} .

APPLICATION QUESTION!

One of the most famous sequences in mathematics is The Fibonacci Sequence. It is defined recursively as follows: $a_n = a_{n-1} + a_{n-2}$; $a_0 = 1$ and $a_1 = 1$. Using this rule, find the first five terms of the sequence.

$$\begin{aligned}
 a_n &= a_{n-1} + a_{n-2} \\
 a_2 &= a_{2-1} + a_{2-2} \\
 a_2 &= a_1 + a_0 \\
 a_2 &= 1 + 1 \\
 a_2 &= 2
 \end{aligned}$$