



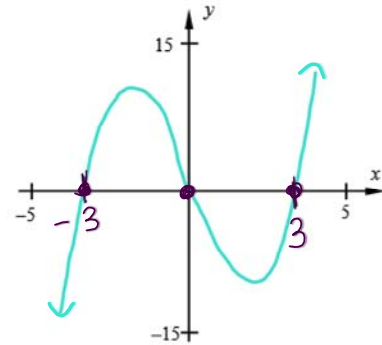
We can even explore higher-order polynomials and their zeroes on a very limited basis. So far the best we have done is an x^2 , but polynomials that contain an x^3 can also be analyzed. These are known as **cubics**.

Exercise #3: Consider the cubic function $f(x) = x^3 - 9x$.

(a) Find the zeroes of this function algebraically by factoring.

$$\begin{aligned}
 x^3 - 9x &= 0 \\
 x(x^2 - 9) &= 0 \\
 x(x-3)(x+3) &= 0 \\
 \boxed{x=0} \quad \boxed{x-3=0} \quad \boxed{x+3=0} \\
 &\quad \quad \quad \boxed{x=3} \quad \quad \quad \boxed{x=-3}
 \end{aligned}$$

(b) Use your calculator to sketch a graph of this function. Circle the zeroes on the graph.



You will study higher-order polynomial functions in Algebra II. But, you should be able to find the zeroes for a limited number of **cubic polynomials** that can be easily factored. In our last exercise, we'd like to explore the relationship between the **zeroes of a quadratic** and the x -coordinate of its turning point.

★ **Exercise #4:** Consider the quadratic $y = x^2 - 8x + 15$.

(a) Find the zeroes of this function algebraically using factoring.

$$\begin{aligned}
 &5 \text{ and } 3 \\
 &-5 \text{ and } -3 \\
 x^2 - 8x + 15 &= 0 \\
 (x-5)(x-3) &= 0 \\
 \boxed{x=5} \quad \boxed{x=3}
 \end{aligned}$$

(b) Write the quadratic function in vertex form and identify the coordinates of its turning point.

$$\begin{aligned}
 -\frac{8}{2} &= (-4)^2 \\
 &= 16 \\
 x^2 - 8x + 15 &= x^2 - 8x + 16 - 16 + 15 \\
 y &= (x-4)^2 - 1 \\
 \text{T.P.} &\rightarrow (4, -1)
 \end{aligned}$$

(c) What is true about the x -coordinate of the turning point compared to the zeroes you found in (a)?

x -coordinate of turning point $\rightarrow 4$
 zeroes $\rightarrow 3$ and 5

(d) Without using a calculator, sketch a graph of this quadratic on the axes below.

