Name: Date:

SQUARE ROOTS HOMEWORK

1. Simplify each of the following. Each will result in a rational number answer. You can check your work using your calculator, but should try to do all of them without it.

(a)
$$\sqrt{36}$$

(b)
$$-\sqrt{4}$$

(c)
$$\sqrt{121}$$

(d)
$$\sqrt{\frac{1}{9}}$$

(e)
$$-\sqrt{100}$$

(f)
$$\sqrt{\frac{81}{36}}$$

(g)
$$-\sqrt{\frac{1}{16}}$$

(h)
$$-\sqrt{144}$$

Find the final, simplified answer to each of the following by evaluating the square roots first. Show the steps that lead to your final answers.

(a)
$$\sqrt{9} + \sqrt{25} - \sqrt{64}$$

(b)
$$5\sqrt{4} + 2\sqrt{81}$$

$$\textcircled{0}^{\frac{2\sqrt{25}+2}{3}}$$

$$2 \cdot 5 + 2 = \frac{10+2}{3} = \frac{12}{3} = 4$$

(d)
$$\sqrt{\frac{1}{4}} \left(\sqrt{121} - \sqrt{9} \right)$$

All of the square roots so far have been "nice." We will discuss what this means more in the next lesson. We can use the Multiplication Property to help simplify certain products of not-so-nice square roots.

3. Find each of the following products by first multiplying the radicands (the numbers under the square roots).

(a)
$$\sqrt{2} \cdot \sqrt{50} =$$

(b)
$$\sqrt{3} \cdot \sqrt{12} =$$

(c)
$$5\sqrt{6} \cdot \sqrt{24} =$$

(d)
$$\sqrt{25} - \sqrt{2} \cdot \sqrt{8} =$$

(e)
$$\sqrt{\frac{1}{2}} \cdot \sqrt{\frac{1}{18}} =$$

(f)
$$\sqrt{\frac{3}{4}} \cdot \sqrt{\frac{27}{4}} =$$

100

4. Write each of the following in simplest radical form. Show the work that leads to your answer. The first exercise has been done to remind you of the procedure.

(a)
$$\sqrt{162} =$$

$$= \sqrt{81} \cdot \sqrt{2}$$

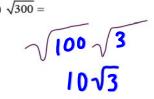
$$= 9\sqrt{2}$$

$$\begin{array}{cccc}
\hline
2 & = & & & \\
& = \sqrt{81} \cdot \sqrt{2} & = & \\
& = 9\sqrt{2} & & & & \\
\hline
2 & \sqrt{5} & & \\
\hline
\end{array}$$

(b)
$$\sqrt{20} =$$
 $\sqrt{4} \sqrt{5}$
 $\sqrt{5}$
 $\sqrt{90} =$
 \sqrt

(d)
$$\sqrt{48} =$$
 (e) $-\sqrt{8} =$ (f) $\sqrt{300} =$ $-\sqrt{4}\sqrt{2}$ $\sqrt{4}\sqrt{3}$ $-2\sqrt{2}$

$$\begin{array}{c}
\text{(e)} -\sqrt{8} = \\
-\sqrt{4} \sqrt{2} \\
-2 \sqrt{2}
\end{array}$$



5. Write each of the following products in simplest radical form. The first is done as an example for you.

(a)
$$3\sqrt{12} =$$

$$= 3 \cdot \sqrt{4} \cdot \sqrt{3}$$

$$= 3 \cdot 2 \cdot \sqrt{3}$$

$$= 6\sqrt{3}$$

(b)
$$4\sqrt{45} =$$

(c)
$$\frac{1}{2}\sqrt{32} =$$

(d)
$$-2\sqrt{288} =$$

(e)
$$\frac{\sqrt{108}}{3}$$
 =

(f)
$$\frac{-\sqrt{320}}{16}$$
 =

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IRRATIONAL NUMBERS

3:5

The set of real numbers is made up of two distinctly different numbers. Those that are **rational** and those that are **irrational**. Their technical definitions are given below.

RATIONAL AND IRRATIONAL NUMBERS

- 1. A rational rumber is any number that can be written as the ratio of two integers. Such numbers include $\frac{3}{4}$, $\frac{-7}{3}$, and $\frac{5}{1}$. These numbers have terminating or repeating decimals.

Exercise #1: Let's consider a number that is rational and one that is irrational (not rational). Consider the rational number $\frac{2}{3}$ and the irrational number $\sqrt{\frac{1}{2}}$. Both of these numbers are less than 1.

(a) Draw a pictorial representation of $\frac{2}{3}$ on the rectangle shown below.



- (c) Write out all of the decimal places that your calculator gives you for $\sqrt{\frac{1}{2}}$. Notice that it does not have a repeating decimal pattern.
- (b) Using your calculator, give the decimal representation of the number $\frac{2}{3}$. Notice that it has a repeating decimal pattern.



(d) Why could you not draw a pictorial representation of $\sqrt{\frac{1}{2}}$ that way you do for $\frac{2}{3}$?

. 7071067812 — mis number cannot be represented as a RATIO

Irrational numbers are necessary for a variety of reasons, but they are somewhat of a mystery. In essence they are a number that can never be found by **subdividing** an **integer quantity** into a **whole number** of **parts** and then taking an **integer number** of those parts. There are many, many types of irrational numbers, but **square roots of non-perfect squares** are **always irrational**. The proof of this is beyond the scope of this course.

Exercise #2: Write out every decimal your calculator gives you for these irrational numbers and notice that they never repeat.

(a)
$$\sqrt{2} = 1.414213562$$
 (b) $\sqrt{10} = 3.16227766$ (c) $\sqrt{23} = 4.795831523$

$$\sqrt{6} = 3$$

$$\sqrt{16} = 4$$

Rational and irrational numbers often mix, as when we simplify the square root of a non-perfect square.

Exercise #3: Consider the irrational number $\sqrt{28}$.

(a) Without using your calculator, between what two consecutive integers will this number lie? Why?

(b) Using your calculator, write out all decimals for

5.291502622

(c) Write $\sqrt{28}$ in simplest radical form.

(d) Write out the decimal representation for your answer from (c). Notice it is the same as (b).

O.k. So, it appears that a non-zero rational number times an irrational number (see letter (c) above) results in an irrational number (see letter (d) above). We should also investigate what happens when we add rational numbers to irrational numbers (and subtract them).

Exercise #4: For each of the following addition or subtraction problems, a rational number has been added to an irrational number. Write out the decimal representation that your calculator gives you and classify the result as rational (if it has a repeating decimal) or irrational (if it doesn't).

(a)
$$\frac{1}{2} + \sqrt{2}$$
 (b) $\frac{4}{3} + \sqrt{10}$ (c) $7 - \sqrt{8}$ (l) $9 + 4 + 17 = 13562$ (e) $4 + 4 = 17 = 1572875$

Exercise #5: Fill in the following statement about the sum or rational and irrational numbers.

When a rational number is added to an irrational number the result is always

Exercise #6: Which of the following is an irrational number? If necessary, play around with your calculator to see if the decimal representation does not repeat. Don't be fooled by the square roots.

(1)
$$\sqrt{25} = 5$$

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IRRATIONAL NUMBERS HOMEWORK									
1.	For each of the following rational numbers, use your calculator to write out either the terminating decimal or the repeating decimal patterns.								
	(a) $\frac{3}{4}$	(b) $\frac{4}{9}$	(c) $\frac{5}{8}$	(d) $\frac{5}{6}$					
	(e) $\sqrt{\frac{25}{4}}$	(f) $\sqrt{\frac{1}{100}}$	(g) $\sqrt{\frac{4}{9}}$	(h) $\sqrt{\frac{2}{32}}$					
2.	 One of the most famous irrational numbers is the number pi, π, which is essential in calculating circumference and area of a circle. (a) Use your calculator to write out all of the decimals your calculator gives you for π. Notice no repeating pattern. (b) Historically the rational number 22/7 has be used to approximate the value of π. your calculator to write out all of the decim for this rational number and compare it to (a) 								
3.	For each of the following irrational numbers, do two things: (1) write the square root in simplest radical form and then (2) use your calculator to write out the decimal representation. (a) $\sqrt{32}$ (b) $\sqrt{98}$ (c) $\sqrt{75}$								
	(d) √500	(e) √80		(f) √117					

Types of numbers mix and match in various ways. The last exercise shows us a trend that we explored during the lesson.

	Fill in the statement helo	1 1 41 1	4:41	- C 41 1- 1- 1-	.1 41 1-1 1-
4	Hill in the statement help	w haced on the lac	t evercise with one	of the words he	NOW the highly

The product of a (non-zero) rational number and an irrational number results in a(n) _____ number

Now we will explore other patterns in the following exercises.

- 5. Let's explore the product of two irrational numbers to see if it is always irrational, sometimes irrational, sometimes rational, or always rational. Find each product below using your calculator (be careful as you put it in) and write out all decimals. Then, classify as either rational or irrational.
 - (a) $\sqrt{5} \cdot \sqrt{3} =$

Rational or irrational?

(b) $\sqrt{8} \cdot \sqrt{18} =$

Rational or irrational?

(c) $\sqrt{7} \cdot \sqrt{11} =$

Rational or irrational?

(d) $\sqrt{11} \cdot \sqrt{11} =$

Rational or irrational?

6. Based on #5, classify the following statement as true or false:

Statement: The product of two irrational number is always irrational. True or False

Let's explore adding rational numbers. Using what you learned about in middle school, add each of the
following pairs of rational numbers by first finding a common denominator then combine. Then,
determine their repeating or terminating decimal.

(a)
$$\frac{1}{2} + \frac{2}{3} =$$

(b)
$$\frac{3}{4} + \frac{1}{2} =$$

(c)
$$\frac{3}{8} + \frac{5}{12} =$$

(d) Classify the following statement as true or false:

Statement: The sum of two rational numbers is always rational. True or False

8. Finally, what happens when we add a rational and an irrational number (we explored this in Exercises #4 through #6 in the lesson). Fill in the blank below from what you learned in class.

The sum of a rational number with an irrational number will always give a(n) _____ number.

rational irrational